Year 1 Key **Representations** Find out more...

Watch the Unit tutorial before planning each unit.

Read the **planning guides** for suggestions of representations.

Make use of PD videos on unit pages and Progression in Calculations page.



Equations

The phrase 'is equal to' is used consistently to refer to the = symbol. What is on one side of the symbol is equal to what is on the other side. Present equations in different ways to support this:

2 + 3 = 55 = 3 + 2

Counting principles – conservation of number

A key number principle for developing addition and subtraction strategies is to understand that the same number of objects will always have the same value.



There are still seven counters. The position has changed but no counters have been added or taken away.

Developing fraction language

The foundations for fractions have been laid through exploration of half full / half empty and associated descriptions. Pupils have also explored doubling and halving without linking specifically to fractions.



The bottle is half full. The bottle is half empty.

Representations of number

Ordering numbers

Comparing numbers

to-one correspondence.

Pupils are most familiar with concrete representations of number within 20 which show one to one correspondence, such as cubes, counters, bead strings to 20 and other countable objects. They also recognise numerals and numbers to 20. A ten frame has been used to represent numbers and think about what this shows.

Pupils have explored a number of ways to order and compare numbers practically using representations including a number track and a number

There are seven counters.

Seven is two more than five.

Seven is three less than 10.

line, within 20. These representations are used to secure counting within 20 and stating one more / one less.

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Concrete representations are used to compare numbers, focusing on

comparison: lining towers of cubes next to one another builds on one-

Counting principles – subitising

faces, triangle shapes can support this.

Subitising is the ability to identify a group of objects without the

need to count. Pupils have explored this and should be confident

correct language use. The structure of the representation supports

Five is less than seven. Five ones is fewer than

seven ones.

Seven is greater than five.

There are 11 cubes. 11 is one more than ten.



representations

5

5

Pupils will have had lots of experience partitioning numbers in different ways through exploring concrete representations. They may identify these as parts and should see that numbers can be split in different ways.

Part-whole language and

A part-whole model is used to represent number bonds, addition and subtraction. Pupils are familiar with the concept of a whole and partitioning this into two or more parts. They explore how to write this relationship as an equation.

The whole is five. I can

partition five into one

part of three and one

part of two.

There are three people

in one train carriage and

two people in another.

One part is three and

one part is two. The

whole is five.



Representing numbers 11-20

Pupils say, read and write teen numbers. Pupils understand the ten and ones relationship of teen numbers, supported by representations.

000000000000000

There are fourteen cubes. This is written as 14. 14 is one ten and four ones.

Doubling and halving

Pupils have had opportunities to represent doubling and halving within 20 practically using manipulatives and other countable objects. Some facts may be

Half of six is three.

Pupils are familiar with addition and subtraction (taking away) using concrete and pictorial representations. A range of contexts for this have been explored. Pupils should be familiar with strategies including count all, count on and count back using representations. 8 9 9 8 9 8

Addition and subtraction strategies

I have three red cubes and four purple cubes. I can put them together and count the whole. There are seven cubes.

I have four yellow cubes. I add two green cubes. I can

count on from four: five, six. There are six cubes.

I have five cubes. I can take away two: four, three. Five take away two is three.



Development of division

Pupils explore counting in equal groups using manipulatives or pictorial representations.

whole = part + part

5 = 3 + 2



0

There are three equal groups of 10. 10, 20, 30. There are 30 altogether.

Pupils have explored the concept of equal and unequal grouping and sharing in context using concrete manipulatives.



15 cows can be grouped into five fields in this way. The groups are unequal.



If 15 bags of grain are shared equally between five farmers, each farmer gets three bags.





equal parts. One quarter is one of four equal parts.



Year 3 Key **Representations** Find out more...

Watch the Unit tutorial before planning each unit and read the Unit Narrative.

Read the **planning guides** for suggestions of representations.

Make use of **PD videos** on unit pages and Progression in Calculations page.

Explore the guidance for Year 3 representations.



Dienes equipment

Number lines

Year 3.

An important resource for demonstrating the relative size of place value columns. Supports the process of regrouping – one ten is equal to ten ones, one hundred is equal to ten tens and so on. Can also be used to represent addition and subtraction with 2- and 3-digit integers.

Number lines can be used to represent and compare numbers and can be used alongside a bead string. They demonstrate the continuous nature of

the number system. When calculating, number lines may act as a jotting of the steps of a mental calculation and may begin 'empty' i.e. not have

numbered divisions. Pupils will have experienced this most through adding tens then ones as shown. The use of number lines is extended during

Pupils use known facts such as number bonds

If I know 12 + 5 = 17 then 22 + 5 = 27.

If I know 12 + 5 = 17 *then* 17 - 12 = 5

If I know 17 - 12 = 5 then 37 - 12 = 25

and understanding of place value and

magnitude to derive further facts.

One ten is regrouped for ten ones. Ten ones is regrouped for one ten.







234 is two hundreds, three tens and four ones. I can represent subtracting 20 by removing two ten sticks.

+2

+20

Bead strings help support the ordinality of

the value 101-200 for representation when

number. They are repurposed e.g. beads have

Bead strings

rounding.

Part-whole language and representations

A part-whole model is used to represent the relationship between numbers in all four operations. The model is made of a whole and two or more parts.



The whole is ten. One part is six and one part is four. Six plus four is equal to ten.

By moving the manipulatives the model represents subtraction.



The whole is ten. I subtract one part of six. The missing part is four. Ten subtract six is equal to four.

Multiplication, division and fractions of quantities can be represented using multiple equal parts.



Bar models

Pictorial bar models and concrete Cuisenaire as bar models are used throughout the year and represent partwhole relationships and knowns and unknowns within problems. See PD videos for further exemplification.



I know the whole is 346, and one of the parts is 112. I do not know the value of the missing part. I can subtract 112 from 346.



The value of each part is 7 and there are 6 equal parts. The whole is unknown. $7 \times 6 = 42$

Equations

The phrase 'is equal to' is used consistently to refer to the = symbol. Equations should be presented with symbols and missing numbers in different positions:

> 38 = 25 + 132 = 37 + 44 $12 \div 2 = 4$

The 'make 10' strategy

Pupils apply number bonds to 10 to calculate how many more/less to the next multiple of ten. They partition the part into two parts to calculate mentally. Using concrete or pictorial representations can scaffold thinking.

36 + 27 = ? I can partition 27 into 4 and 23. 36 plus 4 is equal to 40. 40 plus 23 is equal to 63.



Representing fractions

A range of concrete and pictorial representations are used for fractions including fractions of a whole, as part of a set of objects and as part of a quantity such as a length or volume. Pupils should be familiar with a range of representations.



Concrete and pictorial arrays demonstrate the commutativity of multiplication and inverse relationship of multiplication and division. Pupils should be familiar with considering rows and columns. Part-whole language may be used alongside.

> There are four parts/groups each with a value of three. The whole is 12. Four multiplied by three is equal to 12.

The whole is 12. There are three parts/groups each with a value of 4. 12 divided by three is equal to four. One third of 12 is equal to four.



Place value charts

Place value charts have been used to represent two-digit numbers and can be used alongside concrete, pictorial and abstract representations of number to secure understanding of the positional aspect of the number system. Pupils have made use of place value charts when adding two 2-digit numbers and their use is extended in Year 3.



Arrays





Pupils should be increasingly fluent in number bond recall for all numbers to 20. Make use of transitions and Maths Meetings to develop this.

> 17 = 12 + 517 = 11 + 617 = 10 + 7

Round and adjust

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Pupils apply understanding of ordinality of number, recognising when a part or whole is close to a multiple of 10 e.g. 29, 32. They round before calculating, then adjust their answer accordingly. Concrete or pictorial models are used to represent this.

Deriving facts

Year 4 Key **Representations** Find out more...

Watch the Unit tutorial before planning each unit and read the Unit Narrative.

Read the **planning guides** for suggestions of representations.

Make use of **PD videos** on unit pages and Progression in Calculations page.



38 = 25 + 13

 $\Box = 37 + 44$

 $12 \div 2 = 4$



If I know $3 \times 4 = 12$ then I know $6 \times 4 = 24$

If I know 12 + 5 = 17 *then* 17 - 12 = 5

If I know $3 \times 4 = 12$ then I know $12 \div 4 = 3$

Inverse relationships have also been

explored.

597

They are also familiar with multiplication tables for 2, 3, 4, 5, 6, 8 and 10 and related division facts.

Make use of transitions and Maths Meetings to develop this.

 $6 \times 8 = 48$ $48 \div 8 = 6$

Mental strategies

different positions:

Pupils have experienced a range of mental strategies for all four operations, including:

- Applying number bonds to 10 and 100 to calculate how many more/less to the next multiple of ten, extending to 100 and 1000, using the 'make 10' strategy.
- Identifying numbers close to a multiple of ten or 100 e.g. 28, 201 and using a round and adjust strategy, including for multiplication. "If I know 20 x 4 is 80, then 19 x 4 is 76".
- Identifying near doubles for addition. 43 and 45 can be seen as 'double 43 plus two.'
- Subtracting numbers close together in value, through counting on to find the difference.





30 is ten times greater than 3.

123

Representing fractions

A range of concrete and pictorial representations have been used for fractions including fractions of a whole, as part of a set of objects and as part of a quantity such as a length or volume. Pupils can apply these representations to comparing, finding simple equivalence and adding and subtracting with the same denominator, as well as fractions of sets or quantities.



Representing multiplicative relationships

Pupils have represented multiplicative relationships concretely and pictorially, primarily through arrays, Cuisenaire and bar models. A focus on equal parts, the number of equal parts and the value of each part supports understanding of commutativity and inverse relationships. The representations and language structures support written strategies.

> There are four groups each with a value of 3. There are three groups each with a value of 4. I can see three, four times. I can see four, three times.

12 divided into groups of 4 gives three groups 12 shared into four groups gives 3 in each group

Part-whole language and



Cuisenaire as bar models are used to represent part-whole relationships and knowns and unknowns within problems in all four operations. See PD videos for further exemplification.



I know the whole is 346, and one of the parts is 112. I do not know the value of the missing part. I can subtract 112 from 346.



The value of each part is seven and there are six equal parts. The whole is unknown. Six groups of seven is equal to 42. The whole is 42.

